

## Phase Change Problems

## Phase Change Energy

- These values are constant for a certain amount of a substance.
- The energy required to go from solid to liquid is called the heat of fusion ( $H_{fus}$ ).
- The energy required to go from liquid to gas is called heat of vaporization ( $H_{vap}$ ).
- $q = H n$

## Phase change names

- solid to liquid- melting
- liquid to gas- vaporization (boiling)
- gas to liquid- condensation
- liquid to solid- freezing
- solid to gas- sublimation
- gas to solid- deposition
- \*evaporation is also liquid to gas but is a different process

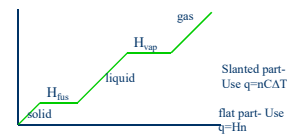
## One way or the other

- Remember melting/freezing point and boiling/condensation point are the same thing.
- The name only implies which way you are going.
- The energy required to melt an object is the same as the energy removed when it freezes.
- The same goes for boiling and condensing.

## New Equation

- $q = nC\Delta T$  is used for problems with a change in temperature
- $q = Hn$  is used for phase changes
- Some problems require both

## Temperature vs. Energy Graph



## Heat of fusion and vaporization

	melting point	Heat of fusion	Boiling point	Heat of vaporization
Water	273 K	6010 J/mol	373 K	40700 J/mol
Nitrogen	63 K	719 J/mol	77 K	5590 J/mol
Lead	601 K	4770 J/mol	2023 K	177800 J/mol

## Problem

- How much energy is required to convert 2.45 moles of solid lead at 601 K to a liquid?
- $q = H_{fus} n$

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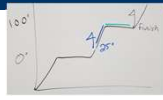
- How much energy is required to convert 2.45 moles of solid lead at 601 K to a liquid?
- $q = H_{fus} n$
- $q = 4770 \text{ J/mol} (2.45 \text{ mol})$
- $q = 11,700 \text{ J}$  or  $11.7 \text{ kJ}$

**A slightly tougher phase change problem**

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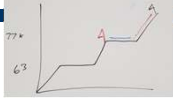
- $q = n C \Delta T + q = H_{\text{vap}} n$
- $q = 3.4 (75.3) 75 + 40700(3.4)$
- 19201 J + 138380 J
- 160,000 J or 160 kJ

**Another**

- How much energy needs to be removed from 1.25 mol of nitrogen at 21° C to make liquid nitrogen at 77 K?

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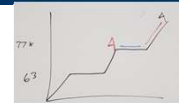
- cool to condensation point (77K- 294K), cool to condense
- $q = 1.25(29.1)(-217) - 1.25(5590)$
- $q = -7890 \text{ J} - 6990 \text{ J}$
- $q = -14880 \text{ J}$

**Problem**

- How much energy needs to be added to 4.7 mol of liquid nitrogen at 77 K to heat it to 291 K?

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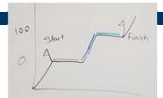
- $q = 4.7(5590) + 4.7 (29.1)(214)$
- $= 55541.78 \text{ J}$
- $q = 56 \text{ kJ}$

**Again**

- How much heat needs to be added to 97.2 mol of 273 K ice to make it to 373 K steam?

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- $q = 6010\text{J/mol} (97.2\text{mol}) + 97.2\text{mol}(75.3\text{J/molK})100\text{K} + 97.2\text{mol}(40700 \text{ J/mol K})$
- $= 5272128 \text{ J}$
- $q = 5.27 \text{ MJ} (5270 \text{ kJ or } 5 \text{ 270 000 J})$

**Another**

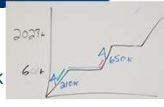
- How much energy needs to be added to 2.7 mol of solid lead at 210 K to heat it to 650 K?

### Another

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- $H_{\text{fus}}$  lead = 4770 J/mol
- $C_{\text{lead}}(\text{solid}) = 26.7 \text{ J/molK}$
- $C_{\text{lead}}(\text{liquid}) = 27.4 \text{ J/molK}$

$q = 2.7 \text{ mol} (26.7) 391\text{K} + 2.7 \text{ mol} (4770) + 2.7 \text{ mol} (27.4)(49 \text{ K})$   
 $= 44691.21 \text{ J}$   
•  $q = 45 \text{ kJ}$



### Last one

- How much heat is required to heat 3.65 mol of ice at  $-15^\circ \text{C}$  to steam at  $120^\circ \text{C}$ ?

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- (heat to melting  $-15$  to  $0$ ) (heat to melt) (heat to boiling  $0$  to  $100$ ) (heat to boil off) (heat to  $100$  to  $120$ )
- $q = 3.65 (38.09) 15 + 3.65(6010)$   
 $+ 3.65(75.3)100 + 3.65(40700) + 3.65(36.8)20$
- $q = 203 \text{ kJ}$

