

## Buffers

### Buffered Solutions.

- A buffered solution is one that resists a change in its pH when either hydroxide ions or protons ( $\text{H}_3\text{O}^+$ ) are added.
- Very little change in pH is witnessed even when a strong acid or base is added.
- The components of a buffer are a conjugate acid-base pair.

### Buffer Calculations

- Assume that the reaction goes to completion, and carry out the *stoichiometric* calculations (based on MOLES).
- Carry out the equilibrium calculations.

### Problems

- Calculate the pH of a buffer of 0.50 M HF and 0.45 M  $\text{F}^-$  (a) before and (b) after the addition of 0.40 g NaOH to 1.0 L of the buffer.
- $K_a$  of HF =  $7.2 \times 10^{-4}$ .

### Answer part (a)

- $\text{HF} \rightleftharpoons \text{H}^+ + \text{F}^-$
- I .50M .45 M
- C -x +x +x
- E.50-x x .45+x
- $K_a = 7.2 \times 10^{-4} = x(x+.45)/(.5-x)$
- $x = [\text{H}^+] = 8.0 \times 10^{-4}$  M
- pH = 3.10

### Answer part (b)

- The sodium hydroxide will react with the HF
- .40 g NaOH  $\times$  1 mol/39.988 g = .010003 mol
- It is 1 L so it is easy to convert to moles
- Assume this reaction goes to completion
- $\text{HF} + \text{OH}^- \rightarrow \text{H}_2\text{O} + \text{F}^-$
- .50 mol .45 mol
- .01 mol
- .49 mol .46 mol
- Now plug these values back into the equilibrium

### Answer part (b) Cont

- $\text{HF} \rightleftharpoons \text{H}^+ + \text{F}^-$
- I .49M .46 M
- C -x +x +x
- E.49-x x .46+x
- $K_a = 7.2 \times 10^{-4} = x(x+.46)/(.49-x)$
- $x = [\text{H}^+] = 7.6 \times 10^{-4}$  M
- pH = 3.12

### Buffers

- Buffered solutions are solutions of weak acids or bases containing a **common ion**.
- The pH calculations on buffered solutions are the same as last chapter.
- When a strong acid or base is added to a buffered solution, do the stoichiometric calculation first.
- Then do the equilibrium calculation.

### How Buffers Work

- The equilibrium concentration of  $\text{H}_3\text{O}^+$ , and thus the pH, is determined by the ratio of  $[\text{HA}]/[\text{A}^-]$ .
- $\text{HA} + \text{H}_2\text{O} \rightleftharpoons \text{A}^- + \text{H}_3\text{O}^+$
- $K_a = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}]}$  so,
- $[\text{H}_3\text{O}^+] = K_a \frac{[\text{HA}]}{[\text{A}^-]}$

### Cont.

- If  $\text{OH}^-$  is added to the system, HA is converted to  $\text{A}^-$ , and the ratio of  $[\text{HA}]/[\text{A}^-]$  decreases.
- However, if the amounts of HA and  $\text{A}^-$  originally present are very large compared with the amount of  $\text{OH}^-$  added, the change in the  $[\text{HA}]/[\text{A}^-]$  ratio will be very small.
- The reverse is true for adding  $\text{H}_3\text{O}^+$  to a system

### The Henderson-Hasselbach Equation.

$$[\text{H}_3\text{O}^+] = K_a \frac{[\text{HA}]}{[\text{A}^-]}$$

$$-\log[\text{H}_3\text{O}^+] = -\log K_a - \log \left( \frac{[\text{HA}]}{[\text{A}^-]} \right)$$

$$\text{pH} = \text{p}K_a - \log \left( \frac{[\text{HA}]}{[\text{A}^-]} \right)$$

$$\text{pH} = \text{p}K_a + \log \left( \frac{[\text{A}^-]}{[\text{HA}]} \right)$$

$$= \text{p}K_a + \log \left( \frac{[\text{C. BASE}]}{[\text{ACID}]} \right)$$

- For a particular buffering system (conjugate base-acid pair), all solutions that have the same ratio  $[\text{A}^-]/[\text{HA}]$  will have the same pH.

### The pH of a Buffered Solution I

- Calculate the pH of a solution containing 0.75 M lactic acid ( $K_a = 1.4 \times 10^{-4}$ ) and 0.25 M sodium lactate. Lactic acid ( $\text{HC}_3\text{H}_5\text{O}_3$ ) is a common constituent of biological systems. For example, found in milk and is present in human muscle tissue during exertion.

### The pH of a Buffered Solution II.

- A buffered solution contains 0.25 M  $\text{NH}_3$  ( $K_b = 1.8 \times 10^{-5}$ ) and 0.40 M  $\text{NH}_4\text{Cl}$ . Calculate the pH of this solution.

### Adding Strong Acid to a Buffered Solution I.

- Calculate the pH of the solution that results when 0.10 mol gaseous HCl is added to 1.0-L of the buffered solution in the previous example.  
\*assume the volume does not change

### Buffer Capacity.

- Buffer capacity represent the amount of protons or hydroxide ions the buffer can absorb without significantly changing the pH.
- The pH of a buffered solution is determined by the ratio of  $[\text{A}^-]/[\text{HA}]$ . The capacity of a buffered solution is determined by the magnitudes of  $[\text{HA}]$  and  $[\text{A}^-]$ .

### Adding Strong Acid to a Buffered Solution II.

- Calculate the change in pH that occurs when 0.0100 mol gaseous HCl is added to 1.0-L of each of the following substances:
  - Solution A: 5.00 M  $\text{HCH}_3\text{COO}$  and 5.00 M  $\text{NaCH}_3\text{COO}$
  - Solution B: 0.050 M  $\text{HCH}_3\text{COO}$  and 0.050 M  $\text{NaCH}_3\text{COO}$
  - Solution C: 0.020 M  $\text{HCH}_3\text{COO}$  and 0.020 M  $\text{NaCH}_3\text{COO}$
- For acetic acid,  $K_a = 1.8 \times 10^{-5}$

### Preparing Buffers

- The most effective buffers have equal concentrations or weak acid to conjugate base or  $[\text{A}^-]/[\text{HA}] = 1$
- $\text{pH} = \text{p}K_a + \log \left( \frac{[\text{A}^-]}{[\text{HA}]} \right)$
- $\log(1) = 0$
- The  $\text{p}K_a$  of the weak acid used should be as close as possible to the desired pH of the buffered solution.

### Preparing a Buffer

- A chemist needs a solution buffered at pH 4.30 and can choose from the following acids and their salts:
  - chloroacetic acid ( $K_a = 1.35 \times 10^{-3}$ )
  - propanoic acid ( $K_a = 1.3 \times 10^{-5}$ )
  - benzoic acid ( $K_a = 6.4 \times 10^{-5}$ )
  - hypochlorous acid ( $K_a = 3.5 \times 10^{-8}$ )
- Calculate the ratio  $[\text{A}^-]/[\text{HA}]$  required to yield the pH 4.30.
- Which system works best?

### Preparing a Buffer II

- How would you prepare a benzoic acid/benzoate buffer with pH 4.25, starting with 5.0-L of 0.050 M sodium benzoate ( $\text{NaC}_6\text{H}_5\text{COO}$ ) solution and adding the acidic component?
- $K_a = 6.3 \times 10^{-5}$  of benzoic acid ( $\text{C}_6\text{H}_5\text{COOH}$ ).